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## Original Paper

# Application of Competition Theory to Tumour Growth: Implications for Tumour Biology and Treatment

R.A. Gatenby

Fels Institute for Cancer Research and Molecular Biology, Temple University School of Medicine, Broad and Ontario Streets, Philadelphia, Pennsylvania 19140, U.S.A.

To assess critical parameters controlling tumour growth and response to therapy, competition theory models the tumour-host interface as a network of interacting normal and malignant cell populations using coupled, non-linear differential equations. When the equations are analysed under conditions which simulate tumour development, three phases of tumour growth, each with different critical parameters, can be predicted. Transitions between these phases correspond to the initiation, promotion and invasion stages demonstrated in experimental models of carcinogenesis. Critical cellular properties for each transition are predicted including phenomena already demonstrated experimentally such as the linkage of invasive tumour growth with acquisition of angiogenesis. The model also predicts the previously unknown phenomenon of "functional equivalence" in which disparate tumour traits can play identical roles in tumour growth and invasion. This approach allows the diverse but inconsistent properties of transformed cells to be understood according to their specific contribution to tumorigenesis. The models have significant implications for treatment strategies. Copyright © 1996 Elsevier Science Ltd

**Key words:** mathematical model, tumour growth, tumour-host interaction

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## INTRODUCTION

CARCINOGENESIS is the consequence of multiple genetic or epigenetic changes. However, no single defect, set of defects, or sequence of defects is observed in all cells exhibiting a transformed morphology [1-3]. Similarly, myriad phenotypic differences have been reported between transformed and normal cells but, as with changes in the genotype, no single property or set of properties is found in all tumour populations [4]. Thus, while multiple genetic, epigenetic and phenotypic differences between normal and tumour cells have been observed, the specific role of each difference in tumorigenesis is frequently obscure. Insignificant, random changes, resulting from the inherent instability of malignant cells, must be distinguished from the critical properties which confer upon a transformed population the characteristics controlling its interaction with the host.

Numerous mathematical models of cancer have been proposed. Some are purely descriptive, such as those which fit tumour growth to Gompertzian [5] or exponential [6] functions. Others are highly mechanistic, generally proposing specific growth controls and examining tumour behaviour within the context of those mechanisms [7-10]. The former

method is limited because it gives no insight into critical parameters for tumour growth, while the latter assumes specific mechanisms and excludes many potentially important areas of tumour biology.

Competition theory provides a novel descriptive framework which also allows examination of critical parameters controlling the tumour-host interface by viewing it as a population invasion analogous to those found in nature [11]. Although normal tissue is a co-operative, non-competitive cellular community, genetic or epigenetic changes in a member of this community will produce a new "tumour" species and new population dynamics. The fate of these transformed individuals depends on a complex web of interactions. For tumorigenesis, transformed cells must evolve properties which allow them to acquire space and resources at the expense of the native populations, despite the numerical advantage of the latter and the inhibitory effects of the host. Thus, competition theory may provide insight into critical factors in the tumour-host interaction, through application of mathematical models of competing populations, already well developed in the discipline of population ecology, to the problem of cancer. Although these models require simplifying assumptions, they have successfully analysed a wide variety of complex population interactions in nature [12-14].

## MATHEMATICAL MODEL

Tumour cells and normal cells are modelled as populations competing for space and other resources in an arbitrarily small

Correspondence to R.A. Gatenby, Temple University Hospital, Department of Diagnostic Imaging, Broad and Ontario Streets, Philadelphia, Pennsylvania 19140, U.S.A.

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volume of tissue within an organ. The heterogeneity of tumour cell societies and the varied cell types present in normal tissue are simplified by assuming that a dominant normal ( $N_2$ ) and tumour population ( $N_1$ ) exist at any given time. A common model of interacting populations is:

$$\frac{dN_1}{dt} = r_1 N_1 \left( \frac{K_1 - N_1 - \alpha_{12} N_2}{K_1} \right) \quad (1)$$

$$\frac{dN_2}{dt} = r_2 N_2 \left( \frac{K_2 - N_2 - \alpha_{21} N_1}{K_2} \right) \quad (2)$$

where  $N_1$  = tumour population,  $N_2$  = the population of normal cells from which the tumour arises,  $r$  = the intrinsic rate of growth for each population,  $K$  = carrying capacity or maximum number of cells from each population which could occupy the tissue space and be adequately supported by the environment in the absence of the competing population,  $\alpha_{21}$  = competition coefficient measuring the effects on  $N_2$  caused by presence of tumour cells  $N_1$ ,  $\alpha_{12}$  = competition coefficient measuring the effects on  $N_1$  caused by presence of  $N_2$ .

Because this interaction can be complex and variable, it is divided into growth inhibitors and stimulators.

$$\alpha_{12} = \alpha_{12i} - \alpha_{12s}$$

with  $\alpha_{12i}$  = quantitation of the host inhibitory effects including immunological response, contact inhibition, induction of terminal differentiation or apoptosis,  $\alpha_{12s}$  = host produced growth factors which stimulate tumour cell growth.

To examine very early tumour growth, equations (1) and (2) can be rewritten and examined under conditions in which  $N_2 = K_2$  and  $N_1$  is very small:

$$\frac{dN_1}{dt} = r_1 N_1 \left( 1 - \frac{N_1}{K_1} - \frac{\alpha_{12}}{K_1} N_2 \right) \quad (3)$$

$$\frac{dN_2}{dt} = r_2 N_2 \left( 1 - \frac{N_2}{K_2} - \frac{\alpha_{21}}{K_2} N_1 \right). \quad (4)$$

For  $N_1$  small ( $N_1 \ll K_1$ ) and  $N_2$  at or near  $K_2$

$$\frac{N_1}{K_1} \approx 0$$

$$\frac{N_2}{K_2} \approx 1.$$

This allows equations (3) and (4) to be reduced to

$$\frac{dN_1}{dt} = r_1 N_1 \left( 1 - \frac{\alpha_{12}}{K_1} N_2 \right) \quad (5)$$

$$\frac{dN_2}{dt} = r_2 N_2 \left( - \frac{\alpha_{21}}{K_2} N_1 \right). \quad (6)$$

The small transformed population will survive only if  $dN_1/dt > 0$  and  $dN_2/dt \leq 0$  for  $N_1$  small and  $N_2$  near  $K_2$ . Using equation (5)

$$\frac{dN_1}{dt} > 0 \text{ only if } 1 - \alpha_{12} N_2 / K_1 > 0 \quad (7)$$

$$\text{and } \alpha_{12} < K_1 / N_2 \quad (8)$$

$$\text{or } \alpha_{12i} - \alpha_{12s} < K_1 / N_2 \quad (9)$$

if  $N_2$  can be approximated as  $K_2$ , then

$$\alpha_{12} < K_1 / K_2 \quad (10)$$

and (6)

$$\frac{dN_2}{dt} \leq 0 \text{ if } \frac{\alpha_{21}}{K_2} \geq 0$$

and thus  $\alpha_{21} \geq 0$ . (11)

This simple analysis yields broad insight into the phenotypic changes required for survival of the transformed clone. First, it defines the requirement that  $\alpha_{21} \geq 0$ . Biologically, this requires that tumour cells do not enhance growth of normal cells.

Equation (9) defines the additional condition necessary for survival of the tumour clone:

$$\alpha_{12s} > \alpha_{12i} - K_1 / N_2. \quad (12)$$

Inspection of this term suggests two phases in early tumour growth. In the period immediately following the initiating genetic events, the clone consists of one or a very small number of cells with no vascular support. Substrate delivery to the clone is dependent on diffusion from surrounding tissue, which results in a smaller carrying capacity than that of vascularised normal tissue ( $K_1 \ll K_2$ ). Under these conditions,  $K_1 / N_2$  is relatively insignificant and equation (9) can be approximated as:

$$\alpha_{12s} > \alpha_{12i}.$$

The biological interpretation of this inequality is that growth of the small tumour clone is entirely dependent on host effects. Thus, initiation will produce a persistent transformed population only if the genetic changes allow the clone to overcome host constraints which restrain growth, such as contact inhibition, immune response, terminal differentiation or induction of apoptosis.

A second phase follows if the surviving clone proliferates because population expansion alters the critical parameters. In this setting, the simplification  $N_1 / K_2 = 0$  and  $N_2 / K_2 = 1$  will not hold since the tumour population is both increasing and causing a decline in the normal population. Biologically, this is analogous to the tumour stage following promoter-induced cell proliferation. It demonstrates that promoters must, therefore, induce population expansion by increasing  $\alpha_{12s}$  which can be accomplished by enhancing the local or systemic production of positive growth factors or increasing the cell's sensitivity to growth factors.

Of particular interest, the value of  $K_1 / N_2$  will progressively increase as the population expands and, when sufficiently large, will dominate the  $\alpha_{12i} - K_1 / N_2$  term. Thus, the models predict that the immunological and non-immunological host constraint of the tumour ( $\alpha_{12i}$ ) will become progressively less effective following promoter-induced expansion. Furthermore, as the  $K_1 / N_2$  term becomes larger, the dependence on stimulation by the host will also decrease (because  $\alpha_{12i} - K_1 / N_2$  will get progressively closer to 0). Thus, tumour behaviour following promotion is largely independent of host generated positive or negative growth factors. However, as shown in

Figure 1 the changes necessary for tumour population survival and expansion are still sufficient only to allow limited, non-invasive tumour growth. This stage is analogous clinically to premalignant lesions (i.e. adenoma, papilloma, or carcinoma *in situ*) because, although the tumour population growth is limited, one or more of its members can acquire an invasive phenotype if additional genetic changes confer cellular properties which fulfill the necessary conditions.

The mathematical models can then be examined to predict phenotypic changes necessary to produce invasive malignant behaviour. This is essentially a search for conditions leading asymptotically to tumour population approaching its carrying capacity ( $K_1$ ) and normal population approaching 0. Requirements for malignant growth can be determined by allowing equations 1 and 2 to approach 0 (an equilibrium state) with the condition that  $N_2$  approaches 0 as the steady state is approached. As  $N_2$  declines,  $\alpha_{12} N_2/K_1$  approaches 0 and equation (3) becomes:

$$\frac{dN_1}{dt} = r_1 N_1 \left( 1 - \frac{N_1}{K_1} \right) \quad (13)$$

For  $dN_1/dt \geq 0$

$$N_1 < K_1$$

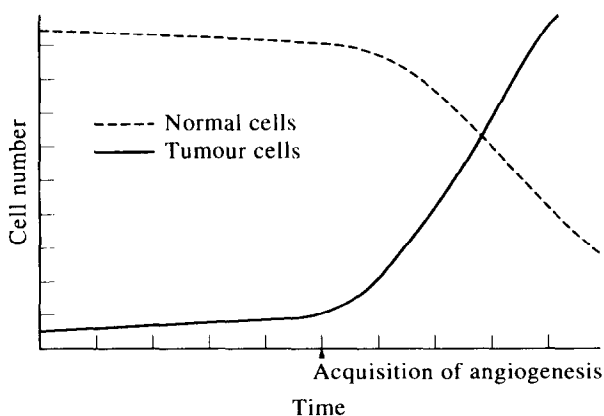
and equation (4) becomes:

$$\frac{dN_2}{dt} = r_2 N_2 \left( \frac{1 - \alpha_{21} N_1}{K_2} \right). \quad (14)$$

For  $dN_2/dt \leq 0$  as  $N_1$  approaches  $K_1$ :

$$\alpha_{21} \geq K_2/K_1.$$

Thus, from the clonal expansion or a pre-malignant stage, an invasive subpopulation will emerge if the clone accumulates phenotypic changes such that the subpopulation displays one of the following strategies: (1) maximise  $\alpha_{21}$ , the effectiveness



**Figure 1.** Computer simulation of population dynamics using equations (1) and (2) during the transition from the clonal proliferation to the malignant stage of tumour growth. Clonal proliferation permits only limited tumour expansion with a significant, persistent population of normal cells. Acquisition of a phenotype which permits invasive growth (as an example, development of an angiogenic phenotype is shown) dramatically alters the population interactions with explosive tumour growth and rapid destruction of the normal tissue.

of the tumour in competing with normal cells for available substrate and space; (2) maximise  $K_1$ , the carrying capacity of the environment for the tumour; (3) minimise  $K_2$ , the carrying capacity for normal cells. Malignant tumour morphology is the final steady state of any of these “strategies” which are, thus, functionally equivalent.

An interesting exception to the constraints on tumorigenesis is seen when transformation occurs in tissue damaged by trauma, infarction or inflammation. This produces initial conditions in which  $N_2 < K_2$ . Thus, in equation (9), the  $K_1/N_2$  term is substantially increased and  $dN_1/dt$  can be  $>0$  under conditions that would have produced  $dN_1/dt < 0$  if  $N_2 = K_2$ . Thus, pre-existing damage to normal tissue creates a cellular ecology relatively permissive for tumour growth.

## DISCUSSION

Competition theory models carcinogenesis as a sequence of steady states resulting from many possible combinations of accumulated genetic or epigenetic changes and with multiple potential outcomes. It predicts the general sequence and types of phenotypic changes necessary for each phase of neoplastic growth, but also demonstrates the novel concept of “functional equivalence”. That is, diverse, apparently unrelated characteristics found in different tumour populations may actually be mathematically and functionally identical in determining tumour behaviour. At any phase of carcinogenesis, one of several interchangeable phenotypes may be sufficient for tumorigenesis and at least one is necessary.

The model demonstrates a sequence of steady states and transitions in carcinogenesis analogous to the initiation, promotion and invasion observed in experimental systems [15, 16]. Each new steady state is dominated by different mathematical parameters which in turn predict critical biological and clinical factors. The first phase occurs immediately after initiation and determines the survival of the altered population. Under these conditions, tumour survival is shown to be dependent solely on host-generated effects. Initiation must, therefore, produce a phenotype with decreased sensitivity to growth constraints such as contact inhibition, terminal differentiation or apoptosis. At this stage, immunological response (a component of  $\alpha_{12i}$ ) can suppress tumour growth, consistent with the concept of immune surveillance.

Increased growth stimulation will result in clonal expansion analogous to the promotion stage of carcinogenesis. This defines the role of the numerous local and systemic factors stimulating tumour growth which have been identified [17–20]. Functionally equivalent properties include increased expression of the growth factor receptors [21–25], which provide persistent stimulation for tumour growth. Alternatively, tumour cells may develop increased responsiveness to, as yet, unknown local factors, such as those produced by normal mesenchyma in bone marrow, or bone resorption products [26–34].

The changes leading to clonal expansion will result in a steady state with limited, unaggressive tumour growth in which tumour and normal cells co-exist. A malignant tumour requires transition to a new state in which the tumour invades host tissue. Several functionally equivalent traits can produce this transition.

First, the tumour could increase its own carrying capacity ( $K_1$ ). Biologically, this is analogous to acquisition of angiogenesis since vascularisation of the tumour population increases substrate delivery and, therefore, the carrying capacity. As

shown in Figure 1, this results in explosive growth of a tumour population, and is consistent with studies of several tumour models, which have shown that non-angiogenic growth is limited, while a change to an angiogenic phenotype results in rapid, unrestricted growth [35–41].

An equivalent strategy to increase  $K_1$  is production of autocrine growth factors which have been shown to increase the maximum obtainable population (the carrying capacity) by as much as a factor of 30 [42].

The second mathematical parameter controlling invasive growth is  $\alpha_{21}$ , which measures the effects of the tumour population on normal cells. In competing, non-predatory populations, the competition coefficient, ( $\alpha$ ), generally represents the deprivation of resources in one population caused by the presence of the other population. Numerous investigators dating back to Warburg [43–46] have observed that tumour cells acquire glucose and other substrate more avidly than normal cells. This asymmetric distribution of resources may be sufficient to produce invasive tumour growth, as the author has previously shown [5].

Finally, a functionally equivalent strategy for invasive growth is reduction of the carrying capacity for normal cells ( $K_2$ ), such as through lysis of the extracellular matrix by proteinases which the tumour produces directly or induces in adjacent fibroblasts [47–49].

Thus, mathematical analysis of tumour growth demonstrates that no single phenotype or set of phenotypes should be expected in all *in situ* neoplasms. The concept of functional equivalence must be employed to understand the highly diverse and inconsistent properties which are observed in tumour populations.

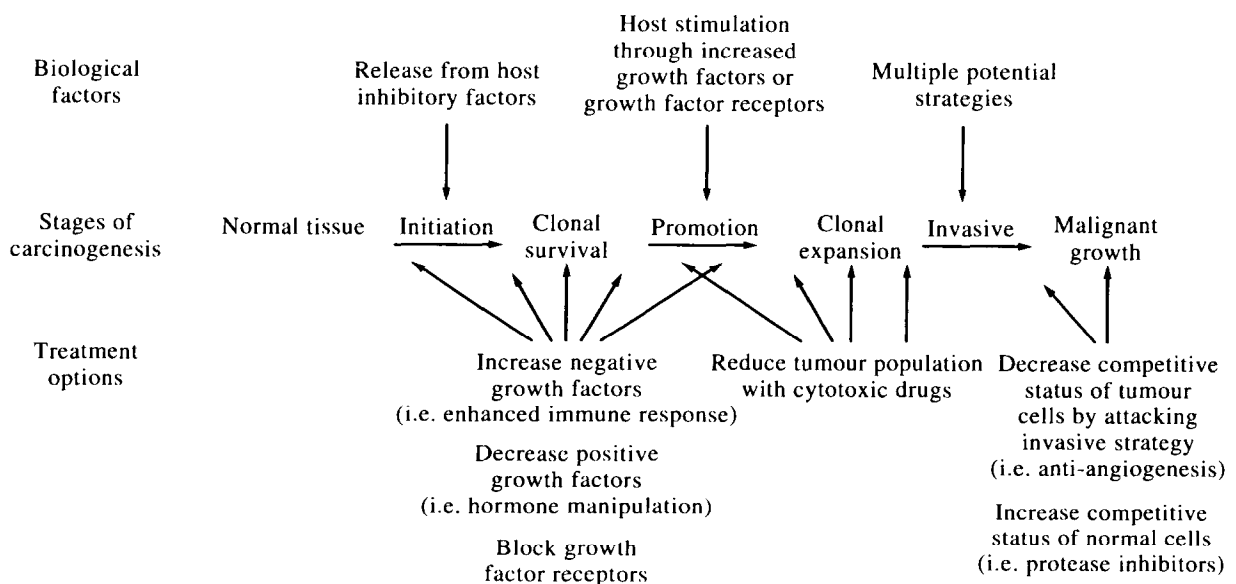
The behaviour of the mathematical models at each stage of tumour growth is dependent on critical parameters which can be “translated” into clinical factors (Figure 2). This allows predictions of treatment strategies likely to be successful or unsuccessful at each phase of tumour growth.

As previously demonstrated, early tumour growth depends on tumour response to host-generated positive and negative growth factors. Thus, tumour prevention or treatment of subclinical (microscopic) tumour (i.e. adjuvant therapy) should exploit this dependence by: (1) reducing the levels of local or systemic growth factors such as through hormonal manipulation, or block their receptors; (2) increasing the immunological response to tumour antigens; and (3) increasing the levels of negative growth factors or receptors.

However, these strategies will be successful only during the early stages of carcinogenesis. As the tumour clone expands, it becomes increasingly independent of host factors, and biological modifiers (i.e. antibodies, cytotoxic lymphocytes, vaccines etc.) will be progressively less successful.

Cytoreduction remains the standard therapy for invasive tumour but inspection of equations (13) and (14) demonstrates significant limitations in this strategy. Tumour is invasive when the parameters of equations (13) and (14) are such that they approach a stable steady state in which tumour population ( $N_1$ ) equals carrying capacity ( $K_1$ ), while the normal population ( $N_2$ ) becomes 0. Under these conditions, the populations will always return to the steady state following perturbations. Thus, the growth term ( $dN_1/dt$ ) will remain positive as long as  $N_1 > 0$ . Clinically, this indicates that the tumour will always repopulate unless the number of tumour cells is reduced to 0. Cytoreductive chemotherapy will always fail in the malignant phase of carcinogenesis unless all of the tumour cells are eradicated.

The mathematical models predict that a more successful strategy would seek solutions to equations (13) and (14) in which  $dN_1/dt = 0$  even if  $N_1 \neq 0$ . This requires treatment that is designed to alter the underlying parameters of the population interaction rather than directly affecting the individual members of the populations and suggests two general approaches: (1) identify the strategy or strategies that the tumour population has evolved in the transition from clonal



**Figure 2.** A summary of the stages of tumour development based on mathematical analysis and their clinical and biological significance. As shown, each stage represents the final result of a transition which is analogous to the initiation, promotion or invasive phase in traditional models of carcinogenesis. The summary outlines critical biological changes which must occur at each transition from one stage to the next. Optimal treatment strategies are also shown as the tumour progresses along the multistep process from initiation of a single cell to invasive growth by billions of cells with death of the host.

expansion to invasive growth and reverse those processes; (2) alter the properties of the normal cells adjacent to the tumour to enhance their competitive status.

1. Cho KR, Vogelstein B. Genetic alterations in the adenoma-carcinoma sequence. *Cancer* 1992, 70, 1727–1731.
2. Weinberg RA. Oncogenes, antioncogenes, and the molecular bases of multistep carcinogenesis. *Cancer Res* 1989, 49, 3713–3721.
3. Bishop JM. The molecular genetics of cancer. *Leukemia* 1988, 2, 199–208.
4. Fidler IJ, Hart IR. Biological diversity in metastatic neoplasms: origins and implications. *Science* 1982, 21, 998–1003.
5. Gatenby RA. Population ecology issues in tumor growth. *Cancer Res* 1991, 51, 2542–2547.
6. Laird AK. Dynamics of tumor growth: comparison of growth rates and extrapolation of growth curves to one cell. *Br J Cancer* 1965, 19, 278–291.
7. Garland H, Coulson W, Wollin E. The rate of growth and apparent duration of untreated primary bronchial carcinoma. *Cancer (Phil.)* 1963, 16, 699–707.
8. Shymko RM. Cellular and geometric control of tissue growth and mitotic instability. *J Theor Biol* 1976, 63, 355–374.
9. Sherratt JA, Nowak MA. Oncogenes, anti-oncogenes and the immune response to cancer: a mathematical model. *Proc R Soc Lond B* 1992, 248, 261–271.
10. Michelson S, Leith JT. Interlocking triads of growth control in tumors. *Bull Math Biol* 1995, 57, 345–366.
11. Wheldon TE. Mitotic autoregulation of normal and abnormal cells: alternative mechanisms for the derangement of growth control. *J Theor Biol* 1975, 53, 421–433.
12. Albrecht F, Gatzke H, Haddad A, Wax N. The dynamics of two interacting populations. *J Math Anal Applic* 1974, 46, 658–670.
13. Goel NS, Maitra SC, Montroll EW. On the Volterra and other nonlinear models of interacting populations. *Rev Modern Phys* 1971, 43, 231–276.
14. Summers D, Wu ZY. Disturbed nonlinear multispecies models in ecology. *Math Biosci* 1991, 104, 185–201.
15. Yuspa SH. The pathogenesis of squamous cell cancer: lessons learned from studies of skin carcinogenesis—thirty-third G.H.A. Clowes Memorial Award Lecture. *Cancer Res* 1994, 54, 1178–1189.
16. Marks F, Furstemberger G. The conversion stage of skin carcinogenesis. *Carcinogenesis* 1990, 11, 2085–2092.
17. Lowry S. Molecular basis for hormone-related cancer. *Lancet* 1993, 41, 1630.
18. Dickson RB, Johnson MD, Bano M. Growth factors in breast cancer: mitogenesis to transformation. *J Steroid Biochem Molec Biol* 1992, 43, 69–78.
19. Geller J. Basis for hormonal management of advanced prostate cancer. *Cancer* 1993, 71, 1039–45.
20. Shroder FH. Endocrine therapy for prostate cancer: recent developments and current status. *Br J Urol* 1993, 71, 633–640.
21. Klijn JGM, Berns PMJJ, Schmitz PIM, Foekens JA. The clinical significance of epidermal growth factor receptor (EGF-R) in human breast cancer: a review on 5232 patients. *Endocrine Rev* 1992, 13, 17.
22. Sainsbury JRC, Nicholson S, Angus B, et al. Epidermal growth factor receptor status of histological sub-types of breast cancer. *Br J Cancer* 1988, 58, 458–460.
23. Berger MS, Greenfield C, Gullick WJ, et al. Evaluation of epidermal growth factor receptors in bladder tumours. *Br J Cancer* 1987, 56, 533–537.
24. Veale D, Kerr N, Gibson GJ, Harris AL. Characterization of epidermal growth factor receptor in primary human non-small cell lung cancer. *Cancer Res* 1989, 49, 1313–1317.
25. Cullen KJ, Lippman ME, Chow D, et al. Insulin-like growth factor-II induces phenotypic changes associated with malignant progression. *Molecular Endocrin* 1992, 6, 91–100.
26. Chackal-Roy M, Niemeyer C, Moore M, Zetter BR. Stimulation of human prostatic carcinoma cell growth by factors present in human bone marrow. *J Clin Invest* 1989, 84, 43–50.
27. Millar-Book W, Orr FW, Singh G. *In vitro* effects of bone- and platelet-derived transforming growth factor-B on the growth of Walker 256 carcinosarcoma cells. *Clin Expl Metastasis* 1990, 8, 503–510.
28. Kostenuik PJ, Singh G, Suyama KI, Orr FW. A quantitative model for spontaneous bone metastasis: evidence for a mitogenic effect of bone on Walker 256 cancer cells. *Clin Exp Metastasis* 1992, 10, 403–410.
29. Cullen KM, Smith HS, Mill S, Rosen W, Lippman ME. Growth factor messenger RNA expression by human breast fibroblasts from benign and malignant lesions. *Cancer Res* 1991, 51, 4978–4985.
30. Miller FR, McEachern D, Miller BE. Growth regulation of mouse mammary tumor cells in collagen gel cultures by diffusible factors produced by normal mammary gland epithelium and stromal fibroblasts. *Cancer Res* 1989, 49, 6091–6097.
31. Hodges GM, Hicks RM, Spacey GD. Epithelial-stromal interactions in normal and chemical carcinogen-treated adult bladder. *Cancer Res* 1977, 37, 3720–3730.
32. Cornil I, Theodorescu D, Man S, Herlyn M, Jambrosic J, Kerebel RS. Fibroblast cell interactions with human melanoma cells affect tumor cell growth as a function of tumor progression. *Proc Natl Acad Sci USA* 1991, 88, 6028–6032.
33. Kabalin JN, Peehl DM, Stamey TA. Clonal growth of human prostatic epithelial cells is stimulated by fibroblasts. *Prostate* 1989, 14, 251–263.
34. Camps JL, Chang SM, Hsu TC, et al. Fibroblast-mediated acceleration of human epithelial tumor growth *in vivo*. *Proc Natl Acad Sci USA* 1990, 87, 75–79.
35. Clarke R, Dickson RB, Brunner N. The process of malignant progression in human breast cancer. *Ann Oncol* 1990, 1, 401–407.
36. Folkman J, Watson K, Ingber D, Hanahan D. Induction of angiogenesis during the transition from hyperplasia to neoplasia. *Nature* 1989, 339, 58–61.
37. Folkman J. The role of angiogenesis in tumor growth. *Cancer Biol* 1992, 3, 65–71.
38. Folkman J, Watson K, Ingber D, Hanahan D. Switch to the angiogenic phenotype during tumorigenesis. In Harris CC, et al, eds. *Multistage Carcinogenesis*. CRC Press, Bolaration, 1991, 339–347.
39. Weidner N, Folkman J, Pozza F, et al. Tumor angiogenesis: a new significant and independent prognostic indicator in early-stage breast carcinoma. *J Natl Cancer Inst* 1992, 84, 1875–1887.
40. Weidner N, Semple JP, Welch WR, Folkman J. Tumor angiogenesis and metastasis—correlation in invasive breast carcinoma. *N Engl J Med* 1991, 324, 1–8.
41. Rastinejad F, Polverini PJ, Bouck NP. Regulation of the activity of a new inhibitor of angiogenesis by a cancer suppressor gene. *Cell* 1989, 56, 345–355.
42. Lippman ME, Dickson RB, Bates S. Autocrine and paracrine growth regulation of human breast cancer. *Breast Cancer Res Treat* 1986, 7, 59.
43. Warburg O. The metabolism of tumours (translated into English by F. Dickens), London, Constable, 1930.
44. Hatanaka M, Huebner RJ, Gilden RV. Alterations in the characteristics of sugar uptake by mouse cells transformed by murine sarcoma viruses. *J Natl Cancer Inst* 1969, 43, 1091–1096.
45. Kalckar HM, Kijimoto US, Hakomori S. Carbohydrate catabolism and the enhancement of uptake of galactose in hamster cells transformed by polyoma virus. *Proc Natl Acad Sci USA* 1973, 70, 839–843.
46. Flier JS, Mueckler MM, Usher P, Lodish HF. Elevated levels of glucose transport and transporter messenger RNA are induced by ras or src oncogenes. *Science* 1987, 235, 1492.
47. Basset P, Bellocq JP, Wolf C, et al. A novel metalloproteinase gene specifically expressed in stromal cells of breast carcinomas. *Nature* 1990, 348, 699–704.
48. Ossowski L. Invasion of connective tissue by human carcinoma cell lines: requirement for urokinase, urokinase receptor, and interstitial collagenase. *Cancer Res* 1992, 52, 6754–6760.
49. Pyke C, Ralfkiaer E, Huhtala P, Hurskainen T, Dano K, Triggvason K. Localization of messenger RNA for M, 72,000 and 92,000 type IV collagenases in human skin cancers by *in situ* hybridization. *Cancer Res* 1992, 52, 1336–1341.